

FIGURE 1-7. Visualization of the spatial and spectral resolutions of the Landsat TM and AVIRIS in the VNIR spectral range. The relative proportions between the two sensors are correct along each axis, and each small rectangular box represents one image pixel. The TM samples the spectral dimension incompletely and with relatively broad spectral bands. In comparison, AVIRIS represents almost a continuous spectral sampling. It also has a somewhat smaller GIFOV. This volume visualization is called an "image cube."

遙測影像處理演算法

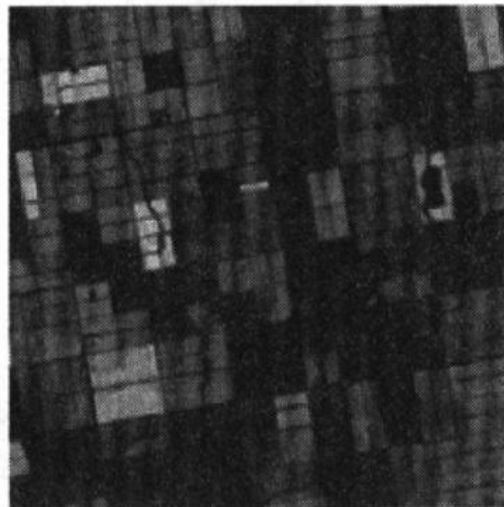
植生指數

Ratio Vegetation Index (RVI)

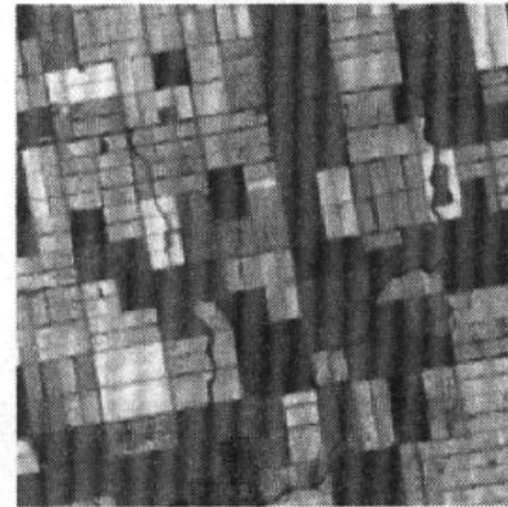
$$RVI = \frac{NIR}{R}$$

Normalized Difference Vegetation Index (NDVI)

$$NDVI = \frac{NIR - R}{NIR + R}$$



RVI



NDVI

FIGURE 5-5. The RVI and NDVI index images for the TM agriculture image of Plate 5-1. Bands 4 and 3 were used and the indexes are calculated from uncalibrated DN's.

PCA

- **Principal Component Analysis**
- 對一組高維度空間中的資料投影到低維度空間
- 找出最佳的投影方式，使得投影後的資料點能盡量散開

假設我們的資料點是由維度為 m 的向量 X_i 來表，
其中 $i = 1, 2, \dots, n$

假設這一組資料的平均值是零：

$$\sum_{i=1}^n X_i = 0$$

目標是要找一個單位向量 \mathbf{u} ，使得在 \mathbf{u} 方向的投影平方和為最大

用一個 $m \times n$ 矩陣 \mathbf{A} 來表示此資料

$$\mathbf{A} = \begin{bmatrix} \mathbf{X}_1 & \mathbf{X}_2 & \mathbf{X}_3 & \cdots & \mathbf{X}_n \end{bmatrix}$$

這一組資料在方向的投影可以表示為下列向量：

$$p = \begin{bmatrix} X_1^T u \\ X_2^T u \\ \vdots \\ X_n^T u \end{bmatrix} = A^T u$$

投影平方的總和為：

$$J(u) = \|p\|^2 = p^T p = (A^T u)^T (A^T u) = u^T A A^T u$$

欲使投影總和為最大，並滿足 $\|u\|=1$ ，
我們可引進Lagrange Multiplier，並形
成新的目標函數：

$$\tilde{J}(u) = u^T A A^T u - \lambda(u^T u - 1)$$

微分取極值 $\nabla_u \tilde{J} = 0 \Rightarrow 2A A^T u - 2\lambda u = 0$

$$\Rightarrow A A^T u = \lambda u$$

根據線性代數

λ 爲 AA^T 的 *eigenvalue*

u 爲 AA^T 的 *eigenvector*

AA^T *eigenvalue* 的大小排列

$$\lambda_1 \geq \lambda_2 \geq \lambda_3 \geq \cdots \geq \lambda_m$$

對應的 *eigenvector* 則是

$$u_1, u_2, u_3 \cdots u_m$$

透過PCA，我們能找出一組單位向量
 $\{ u_1, u_2, u_3 \cdots u_m \}$ ，使得

$$y_i = A^T u_i$$

其中， y_i 稱爲第 i 組主要分量（the i -th principal component）。

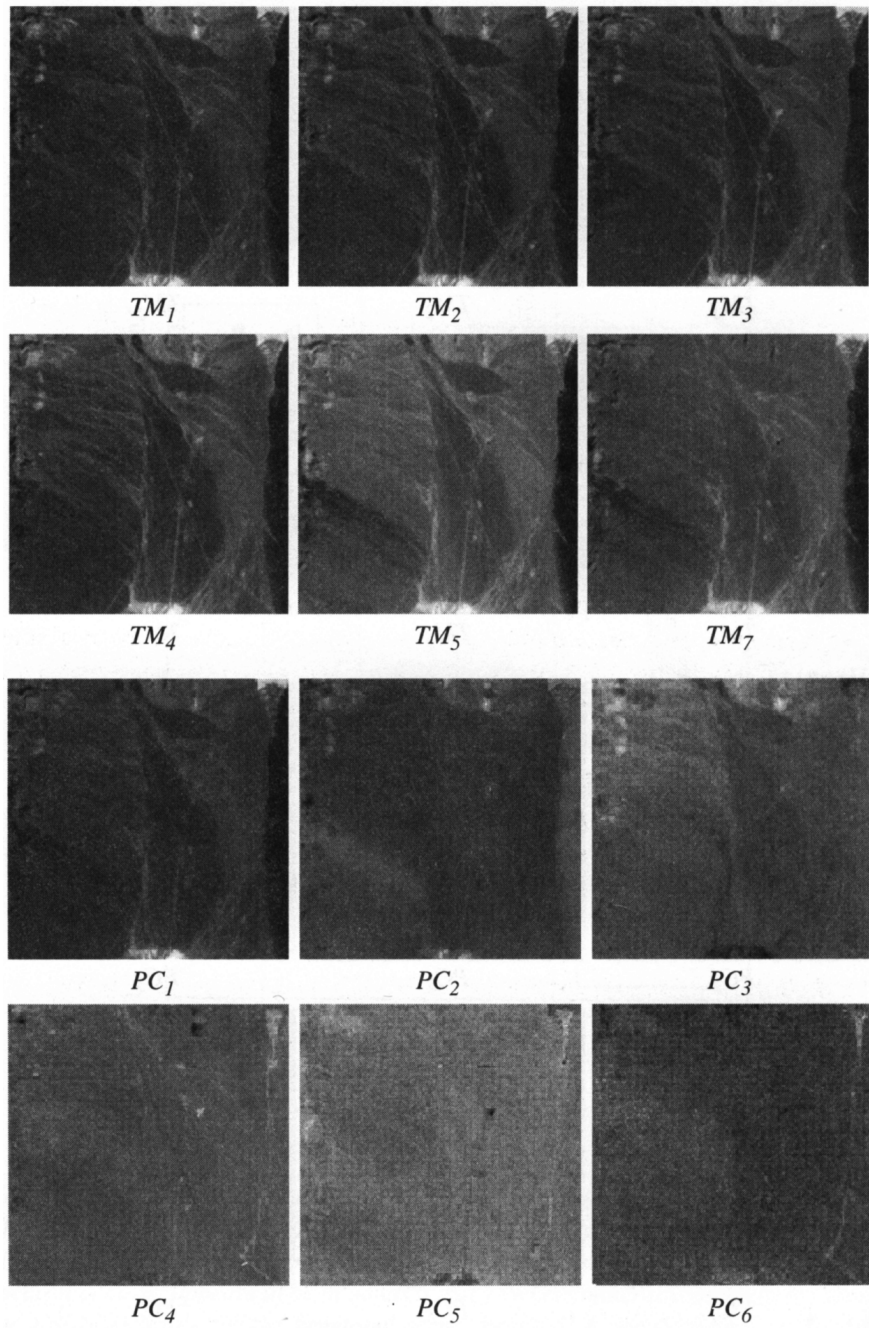
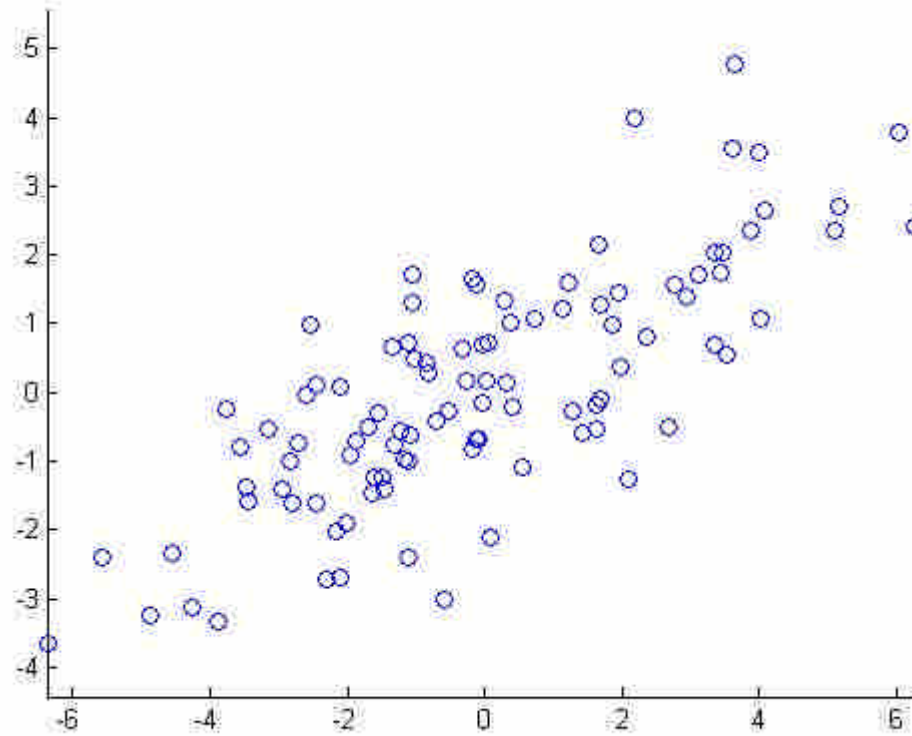


FIGURE 5-13. PC transformation of a nonvegetated TM scene.

Example



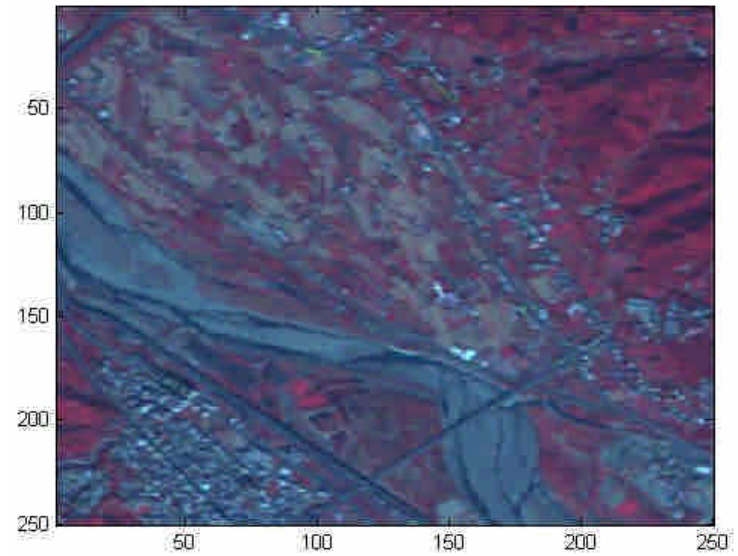
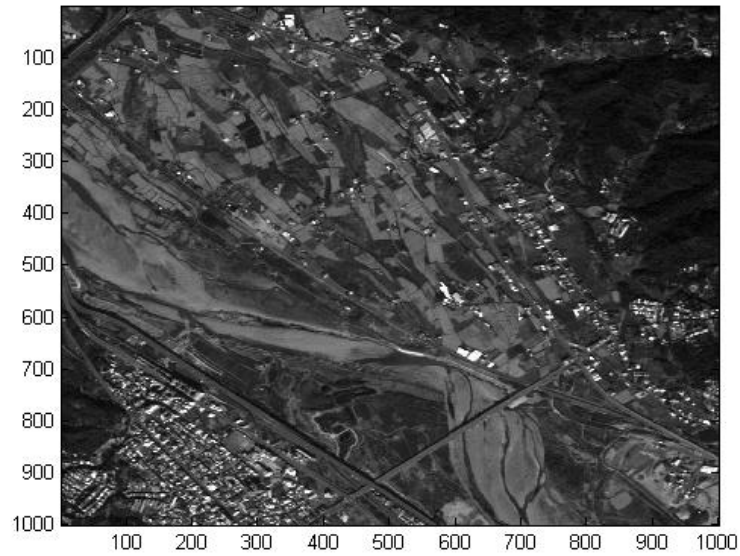
原始資料

sensor	axis name	W_{TC}									
		MSS band				TM band					
		1	2	3	4	1	2	3	4	5	7
L-1 MSS	soil brightness	[+0.433 +0.632 +0.586 +0.264]									
	greenness	[-0.290 -0.562 +0.600 +0.491]									
	yellow stuff	[-0.829 +0.522 -0.039 +0.194]									
	non-such	[+0.223 +0.120 -0.543 +0.810]									
L-2 MSS	soil brightness	[+0.332 +0.603 +0.676 +0.263]									
	greenness	[+0.283 -0.660 +0.577 +0.388]									
	yellow stuff	[+0.900 +0.428 +0.0759 -0.041]									
	non-such	[+0.016 +0.428 -0.452 +0.882]									
L-4 TM	soil brightness	[+0.3037 +0.2793 +0.4743 +0.5585 +0.5082 +0.1863]									
	greenness	[-0.2848 -0.2435 -0.5436 +0.7243 +0.0840 -0.1800]									
	wetness	[+0.1509 +0.1973 +0.3279 +0.3406 -0.7112 -0.4572]									
	haze	[-0.8242 +0.0849 +0.4392 -0.0580 +0.2012 -0.2768]									
	TC5	[-0.3280 +0.0549 +0.1075 +0.1855 -0.4357 +0.8085]									
	TC6	[+0.1084 -0.9022 +0.4120 +0.0573 -0.0251 +0.0238]									
L-5 TM	soil brightness	[+0.2909 +0.2493 +0.4806 +0.5568 +0.4438 +0.1706]									
	greenness	[-0.2728 -0.2174 -0.5508 +0.7221 +0.0733 -0.1648]									
	wetness	[+0.1446 +0.1761 +0.3322 +0.3396 -0.6210 -0.4186]									
	haze	[+0.8461 +0.0731 +0.4640 -0.0032 -0.0492 +0.0119]									
	TC5	[+0.0549 -0.0232 +0.0339 -0.1937 +0.4162 -0.7823]									
	TC6	[+0.1186 -0.8069 +0.4094 +0.0571 -0.0228 +0.0220]									
	soil brightness	[+10.3695]									
	greenness	[-0.7310]									
	wetness	additive terms: [-3.3828]									
	TC5	[+0.7879]									
TC6	[-2.4750]										
		[-0.0336]									

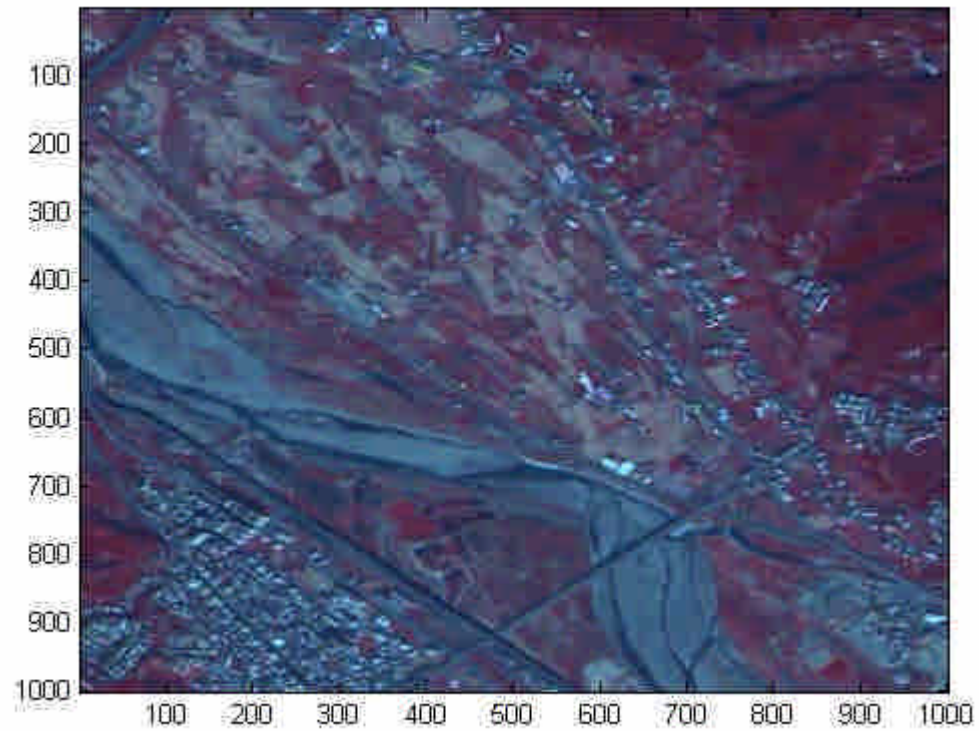
TABLE 5-2. Tasseled-cap coefficients for Landsat-1 MSS (Kauth and Thomas, 1976), Landsat-2 MSS (Thompson and Whemanen, 1980), Landsat-4 TM (Crist and Cicone, 1984) and Landsat-5 TM (Crist et al., 1986). The MSS coefficients are for a 0-63 DN scale in band 4 and a 0-127 DN scale in the other bands, i.e. the same as data supplied to users.

CST

```
load fusion_spot  
imagesc(A)  
colormap(gray)  
figure  
image(A1(:,:, [3 2 1]))
```



CST



```
C=rgb2hsv(B);  
D=zeros(1000,1000,3);  
for i=1:4,for j=1:4  
    D(i:4:end,j:4:end,:)=C;  
end,end  
D(:,:,3)=double(A)/255;  
F=hsv2rgb(D);
```

Color Space Transform

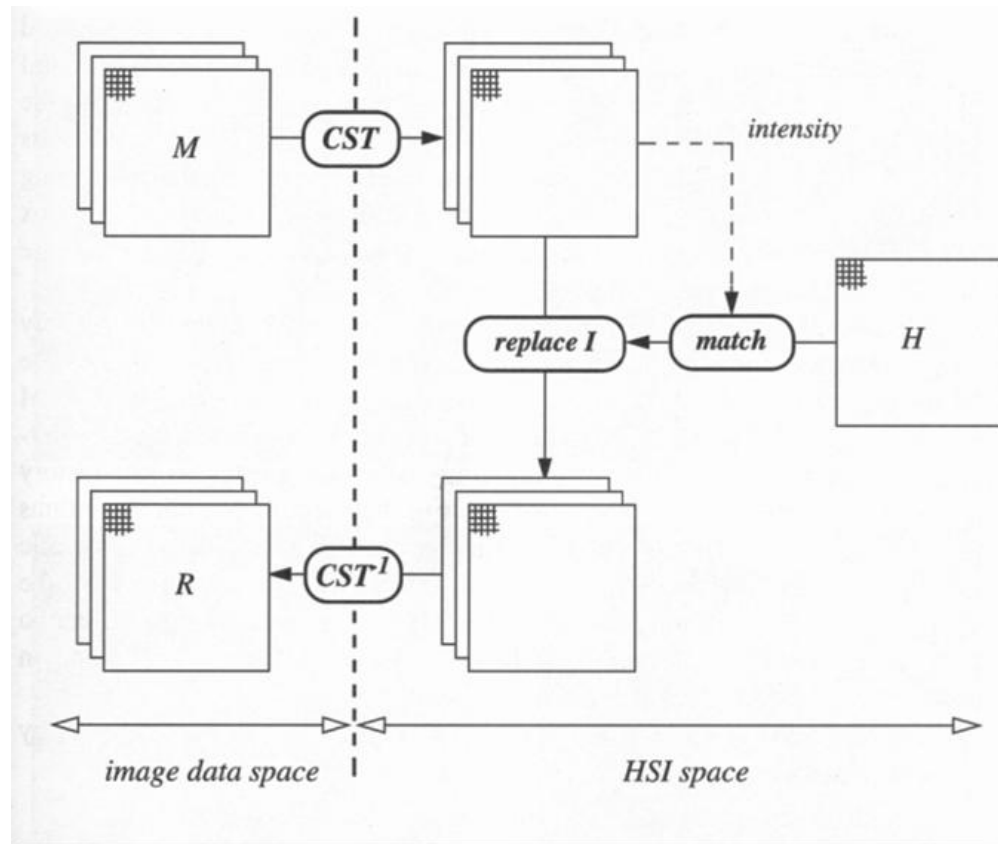


FIGURE 8-14. Image fusion using a color space transform (CST) and replacement of the intensity component. The multispectral image *M* has been previously registered to the high resolution image *H*.